

# Structures and Electronic Properties of $V_3Si_n^-$ ( $n = 3-14$ ) Clusters: A Combined Ab Initio and Experimental Study

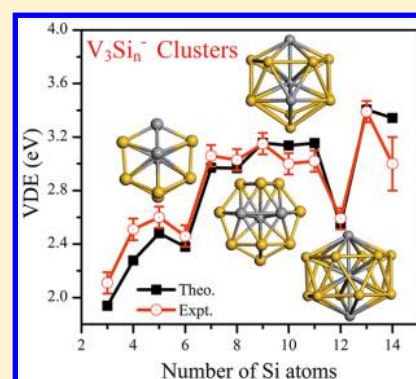
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**ABSTRACT:** Vanadium-doped silicon cluster anions,  $V_3Si_n^-$  ( $n = 3-14$ ), have been generated by laser vaporization and investigated by anion photoelectron spectroscopy. The vertical detachment energies (VDEs) and adiabatic detachment energies (ADEs) of these clusters were obtained. Meanwhile, genetic algorithm (GA) combined with density functional theory (DFT) calculations are employed to determine their ground-state structures systematically. Excellent agreement is found between theory and experiment. Among the  $V_3Si_n^-$  clusters,  $V_3Si_5^-$ ,  $V_3Si_9^-$ , and  $V_3Si_{12}^-$  are relatively more stable. Generally speaking, three V atoms prefer to stay close with others and form strong V–V bonds. Starting from  $V_3Si_{11}^-$ , cage configurations with one interior V atom emerge.



## 1. INTRODUCTION

As the backbone in modern microelectronics industry, silicon is the most important elementary semiconductor. The continuous trend of miniaturization in microelectronics triggers a quest for nanostructured building blocks. Therefore, there have been tremendous interests in Si nanostructures.<sup>1,2</sup> The research of Si clusters was initiated in the 1980s.<sup>3</sup> It is known that the ground-state configurations of Si clusters strongly depend on cluster size and do not resemble the bulk fragments.<sup>4-8</sup> Silicon clusters prefer to form compact three-dimensional geometries via  $sp^3$  hybridization.<sup>9</sup> Unfortunately, elemental silicon clusters tend to have surface dangling bonds, which renders them chemically reactive and therefore not suitable for nanoscale building blocks.<sup>4</sup> In the past decade, it has been shown both theoretically and experimentally that incorporation of transition metal (TM) atoms into a silicon cluster not only stabilizes the cluster but also brings into peculiar physical properties such as high magnetic moments.<sup>10-19</sup>

Previously, the lowest-energy structures, thermodynamic stabilities, and physical properties of small and medium-sized TM-doped  $Si_n$  clusters up to  $n = 20$  have been investigated by ab initio calculations.<sup>10,11,16,20-23</sup> Incorporation of even a single TM atom can lead to stabilization of otherwise unfavorable cage-like silicon structures.<sup>11</sup> The embedding energy of a TM atom (Hf, Zr, Fe, Ru, and Os) is about 12 eV, making the silicon cage stable and compact.<sup>10</sup> Ma et al.<sup>21</sup> showed that Co doping can improve the stability of  $Si_n$  clusters when  $n > 6$ . Wang et al.<sup>24</sup> discussed the most favorable guest

TM atom (TM = Sc–Ni) for  $Si_{15}$  and  $Si_{16}$  cages and found that  $TiSi_n$  have the largest embedding energies and relatively large highest occupied–lowest unoccupied molecular orbital (HOMO–LUMO) gaps.

Particular attentions have been paid to the formation of cage configurations for TM-doped  $Si_n$  clusters with different TM elements.<sup>25-29</sup> For 3d TM elements, a perfect metal encapsulation of  $Si_n$  cage can be achieved at  $n = 16$ , which shows minimum electron affinity and higher stability.<sup>23,25,30,31</sup> It was suggested that  $VSi_{16}^-$  is a fluxional endohedral cage, oscillating around a symmetric Frank-Kasper polyhedral transition state,<sup>15</sup> which has also been confirmed in experiments.<sup>12,14</sup> Due to bigger atom radius with regard to 3d TM, 4d TM elements show a different growing pattern with the TM atoms on the exterior region of silicon cluster.<sup>32,33</sup> For instance, in the  $YSi_n$  clusters, Y atom either locates at the surface site or acts as a linker between two subclusters when  $n < 15$ .<sup>33</sup>

Parallel to the theoretical efforts, there have also been numerous experiments on TM-doped  $Si_n$  clusters ( $n \leq 20$ ), including  $MSi_n$  ( $M = Cr, Mn, Cu, Zn$ ) clusters,<sup>12</sup>  $MSi_{16}$  ( $M = Sc, Ti, V$ ),<sup>14</sup>  $MSi_{16}^-$  ( $M = Ti, Zr, Hf$ ),<sup>34</sup>  $CrSi_{8-12}$ ,<sup>35</sup>  $MSi_n$  ( $M = Sc, Y, Ti, Zr, Hf, V, Nb, Ta$ ),<sup>36</sup>  $MSi_{6-20}^-$  ( $M = Sc, Ti, V, Y, Zr$ ,

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Nb),<sup>37</sup>  $\text{MSi}_n$  ( $M = \text{Ti, Hf, Mo, W}$ ),<sup>38</sup>  $\text{VSi}_{3-6}$ ,<sup>39</sup>  $\text{VSi}_{6-9}^{0,+40}$ ,  $\text{CrSi}_{3-12}^{-28}$ ,  $\text{CuSi}_{4-18}^{-41}$ ,  $\text{AgSi}_{3-12}^{-42}$ . Mass spectra show that  $\text{CrSi}_{15,16}^+$ ,  $\text{MnSi}_{15,16}^+$ , and  $\text{CuSi}_{6,10}^+$  are particularly abundant, which can be attributed to their endohedral structures.<sup>12</sup> The photoelectron spectra reveal that the electron affinities of  $\text{MSi}_n$  exhibit local minima around  $n = 15-16$ .<sup>38</sup> Koyasu et al.<sup>14,36</sup> systematically doped  $\text{Si}_n$  clusters with TM atoms of groups 3, 4, and 5 using a double-laser vaporization method. A prominent peak at  $\text{MSi}_{16}$  was observed in the mass spectra, indicating that species with totally 68 valence electrons are particularly stable. A recent study shows that vanadium atom is doped exohedrally in the silicon clusters and the neutral ones do not differ much from their cationic counterparts.<sup>40</sup>

In contrast to the comprehensive studies on TM-doped  $\text{Si}_n$  clusters with single metal dopant, as discussed above, little is known about multi-TM doped silicon clusters. Intuitively, incorporation of two or more TM atoms would render the structures and properties of  $\text{TM}_m\text{Si}_n$  clusters ( $m \geq 2$ ) more intriguing. Han et al. have systematically investigated the growth pattern of  $\text{Mo}_2\text{Si}_n$  ( $n = 9-16$ ) clusters at (U)B3LYP/LanL2DZ level. They showed that cage-like structures are favorable and the Mo atoms prefer to interact with more silicon atoms.<sup>43</sup> Ji and Luo<sup>44,45</sup> systematically studied cage-like  $\text{M}_2\text{Si}_{18}$  ( $M = \text{Ti-Zn}$ ) clusters using DFT calculations. They found that a double hexagonal prism can form when the doped TM atom has no more than half-full  $d$  electronic shell. Among all 3d doped  $\text{M}_2\text{Si}_{18}$  clusters,  $\text{Co}_2\text{Si}_{18}$  was the most stable one. Xu et al.<sup>39,46,47</sup> reported a combined study of anion photoelectron spectroscopy (PES) and DFT calculations of small  $\text{Si}_n$  clusters doped with two vanadium or scandium atoms. Combining experimental PES and DFT-based structural search, we have recently investigated  $\text{V}_x\text{Si}_{12}^-$  ( $x = 1, 2, 3$ ) and found a ferrimagnetic  $\text{V}_3\text{Si}_{12}^-$  cluster with wheel-like configuration.<sup>48</sup>

To date, silicon clusters doped with three TM atoms have never been investigated (except for our recent study<sup>48</sup>) within the best of our knowledge. As an embryo of TM–Si alloys, it would be interesting to examine the effects of multiple TM atoms on the atomic and electronic structures of doped  $\text{Si}_n$  clusters. In particular, determination of the global minimum geometries of  $\text{TM}_3\text{Si}_n$  clusters is a great challenge due to the coexistence of three TM atoms and consequently numerous possible isomer structures on the potential energy surface. Here we perform a combined study of anion PES and DFT-based global search of  $\text{Si}_n$  clusters (up to  $n = 14$ ) doped with three vanadium atoms. Vanadium ( $[\text{Ar}] 3d^3 4s^2$ ) is chosen as dopant element since it is a 3d transition metal with an open  $d$  shell, which results in moderate reactivity and possible magnetism. It would be interesting to explore the interaction between vanadium dopant and silicon host, especially in the cases of coexistence of multiple metal dopants where the interaction between the metal atoms may interplay with the metal–silicon interaction.

## 2. EXPERIMENTAL AND THEORETICAL METHODS

The experiments were conducted on a home-built apparatus consisting of a laser vaporization cluster source, a time-of-flight mass spectrometer, and a magnetic-bottle photoelectron spectrometer, which has been described elsewhere.<sup>39</sup> The V–Si cluster anions were generated in the laser vaporization source by laser ablation of a rotating translating disk target (13 mm diameter, V/Si mole ratio 1:2) with the second harmonic of a nanosecond Nd:YAG laser (Continuum Surelite II-10). The typical laser power was about 10 mJ/pulse. With  $\sim 4$  atm

helium gas, backing pressure was allowed to expand through a pulsed valve (General Valve Series 9) into the source to cool the formed clusters. The generated cluster anions were mass-analyzed with the time-of-flight mass spectrometer. The cluster anions of interest were size-selected with a mass gate, decelerated by a momentum decelerator, and crossed with the beam of an Nd:YAG laser (Continuum Surelite II-10, 266 nm) at the photodetachment region. The electrons from photodetachment were energy-analyzed by the magnetic-bottle photoelectron spectrometer. The resolution of the magnetic-bottle photoelectron spectrometer was about 40 meV at electron kinetic energy of 1 eV. The photoelectron spectra were calibrated with the spectra of  $\text{Cu}^-$  and  $\text{Au}^-$  ions taken at similar conditions.

Theoretically, the low-lying structures of  $\text{V}_3\text{Si}_n^-$  ( $n = 3-14$ ) cluster anions were globally searched using genetic algorithm<sup>49,50</sup> incorporated with DFT calculations (GA-DFT). In the GA search, 24 initial configurations in the population were generated randomly. During each GA iteration, any two individuals were chosen as parents to produce a child cluster,<sup>50</sup> followed by an optional mutation operation of 50% probability. Three types of mutation operations were adopted here: (1) exerting each atom a small random displacement, (2) moving several selected atoms by small step and keeping other atoms fixed, and (3) exchanging the atomic types of two heteroatoms. The child cluster was then fully relaxed by DFT optimization without symmetry constraint, using DMol<sup>3</sup> program<sup>51,52</sup> with double numerical basis including d-polarization function (DND) and the Perdew–Burke–Erzerhof (PBE) functional within generalized gradient approximation (GGA).<sup>53</sup> Self-consistent field calculations were done with a convergence criterion of  $10^{-6}$  Hartree on the total energy and real-space orbital cutoff of 6.5 Å. The optimized child cluster may enter the population if it has lower energy than an existing member. The diversity of the GA population was ensured by distinguishing the identical configurations in terms of their inertia.<sup>54</sup> For each cluster size, we performed more than 2000 GA iterations to reach global minimum on the potential energy surface. The validity and efficiency of the present GA-DFT scheme have been well demonstrated in our previous studies on  $\text{Ga}_m$ ,<sup>55</sup>  $\text{Na}_m$ ,<sup>56</sup>  $\text{Na-Si}$ ,<sup>54</sup>  $(\text{WO}_3)_m$ ,<sup>57</sup> and  $\text{AuAg}$ <sup>58</sup> clusters. As a successful application, the most stable configurations of neutral and anionic  $\text{Na}_n\text{Si}_m$  ( $n = 1-3$ ,  $m = 1-11$ ) clusters were obtained and the theoretical electronic properties compare well with experimental data.<sup>54</sup>

The accuracy of the present DFT methodology was assessed by benchmark calculations for  $\text{V}_2$  and  $\text{Si}_2$  dimers as well as bulk solids of V and Si. Upon spin-polarized DFT calculation, the  $\text{V}_2$  dimer has  $1 \mu_B$  magnetic moment on each V atom. The calculated V–V bond length (BL) is 1.798 Å, in excellent agreement with experimental value of 1.77 Å.<sup>59</sup> Similarly, the theoretical Si–Si BL of 2.175 Å is comparable to 2.246 Å in experiment.<sup>60</sup> From our DFT calculations, the vibrational frequencies for  $\text{V}_2$  and  $\text{Si}_2$  dimers are 615.9 and 532.1  $\text{cm}^{-1}$ , which compare reasonably with experimental data of 537  $\text{cm}^{-1}$ <sup>59</sup> and 510.98  $\text{cm}^{-1}$ ,<sup>60</sup> respectively. For reference, previous theoretical results of bond length and frequency for  $\text{V}_2$  dimer were 1.797 Å and 630.5  $\text{cm}^{-1}$  at BLYP/DND level.<sup>44</sup> The calculated ionization energies of  $\text{V}_2$  and  $\text{Si}_2$  dimers are 6.549 and 7.823 eV, which are also in line with the experimental data of 6.357 eV<sup>61</sup> and 7.9 eV,<sup>62</sup> respectively. On the other hand, from our calculations, the lattice parameters for silicon (in diamond structure) and vanadium (in bcc structure) solids are

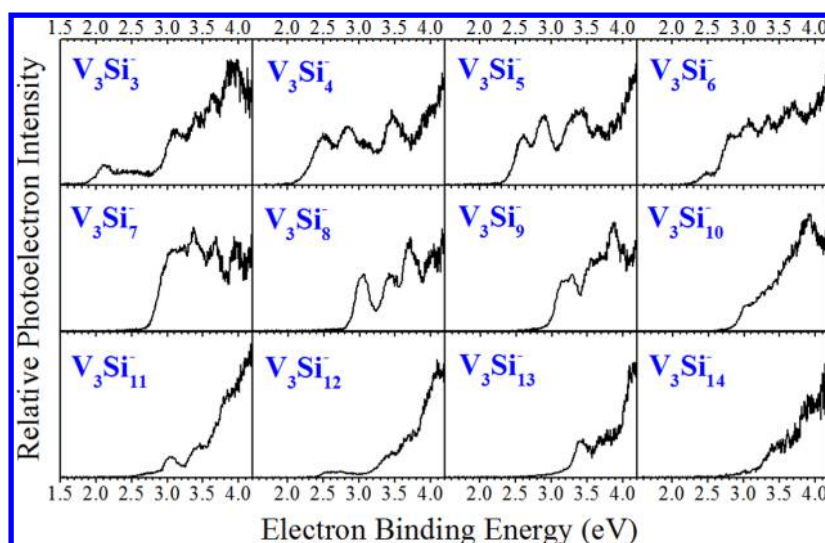


Figure 1. Photoelectron spectra of  $V_3Si_n^-$  clusters ( $n = 3-14$ ) recorded with 266 nm photons.

Table 1. Data of Experimental and Theoretical Vertical Detachment Energies (VDEs) and Adiabatic Detachment Energies (ADEs), Binding Energies ( $E_b$ ), Second-Order Energy Differences ( $\Delta_2E$ ), HOMO-LUMO Gaps of  $V_3Si_n^-$  Clusters are Shown in the Unit of eV

cluster <sup>-</sup>	VDE		ADE		$E_b$	$\Delta_2E$	gap
	expt.	theo.	expt.	theo.			
$V_3Si_3^-$	$2.11 \pm 0.08$	1.94	$1.90 \pm 0.08$	1.76	3.59		0.83
$V_3Si_4^-$	$2.51 \pm 0.08$	2.28	$2.14 \pm 0.08$	2.18	3.75	0.043	1.07
$V_3Si_5^-$	$2.60 \pm 0.08$	2.48	$2.34 \pm 0.08$	2.38	3.86	0.063	0.78
$V_3Si_6^-$	$2.46 \pm 0.08$	2.38	$2.18 \pm 0.08$	2.36	3.91	-0.013	0.61
$V_3Si_7^-$	$3.06 \pm 0.08$	2.97	$2.73 \pm 0.08$	2.75	3.98	0.021	0.93
$V_3Si_8^-$	$3.03 \pm 0.08$	2.97	$2.81 \pm 0.08$	2.89	4.03	-0.004	0.75
$V_3Si_9^-$	$3.15 \pm 0.08$	3.16	$2.96 \pm 0.08$	3.08	4.07	0.057	0.91
$V_3Si_{10}^-$	$3.00 \pm 0.08$	3.14	$2.85 \pm 0.08$	3.04	4.07	-0.027	1.08
$V_3Si_{11}^-$	$3.02 \pm 0.08$	3.16	$2.84 \pm 0.08$	3.08	4.09	-0.008	1.06
$V_3Si_{12}^-$	$2.59 \pm 0.08$	2.54	$2.44 \pm 0.08$	2.53	4.11	0.024	0.34
$V_3Si_{13}^-$	$3.39 \pm 0.08$	3.41	$3.07 \pm 0.08$	3.31	4.12	0.013	0.80
$V_3Si_{14}^-$	$3.00 \pm 0.2$	3.34	$2.90 \pm 0.2$	3.21	4.11		0.39

5.47 and 3.10 Å, respectively, and the cohesive energies for Si and V solids are 4.56 and 5.34 eV/atom, respectively. For comparison, the experimental lattice constants are 5.43 and 3.03 Å for Si and V solids, and the corresponding cohesive energies are 4.63 and 5.31 eV/atom, respectively.<sup>63</sup> In short, our PBE/DND scheme is able to describe the structural and bonding properties of V and Si systems in a satisfactory manner.

### 3. RESULTS AND DISCUSSION

**3.1. Photoelectron Spectra of  $V_3Si_n^-$  ( $n = 3-14$ ) Clusters.** Figure 1 displays the photoelectron spectra of  $V_3Si_n^-$  clusters ( $n = 3-14$ ) recorded with 266 nm (4.661 eV) photons. Each peak of the PES represents a transition from the ground state of the cluster anion to the ground or an excited state of their corresponding neutrals. To account for the broadening of the photoelectron spectra peaks due to the instrumental resolution, the ADE of each cluster was estimated by adding the value of the instrumental resolution to the electron binding energy at the crossing point between the baseline and the leading edge of the first peak. The VDE was estimated from the maximum of the first peak.

The spectrum of  $V_3Si_3^-$  has a small peak at around 2.11 eV, which gives the VDE. After this, there is a broadened area and several peaks between 3 and 4 eV. The VDE of  $V_3Si_4^-$  is about 2.51 eV. The front two peaks of the PES are close to each other, while the third one locates at about 3.5 eV. The spectrum of  $V_3Si_5^-$  is similar to that of  $V_3Si_4^-$  and the VDE is about 2.60 eV. For  $V_3Si_6^-$ , the first peak is very small and shows a little broadening, corresponding to a VDE of 2.46 eV. The successive five peaks become increasingly higher. The spectrum of  $V_3Si_7^-$  exhibits a broad feature between 2.9 and 3.3 eV with three major peaks centered at 3.36, 3.66, and 3.95 eV. Four well-resolved peaks centered at 3.03, 3.44, 3.69, and 4.05 eV are evident in the spectrum of  $V_3Si_8^-$ . For  $V_3Si_9^-$ , there are two broad features at 3.2–3.4 eV and 3.5–4.1 eV plus a narrow peak at 3.88 eV. In the case of  $V_3Si_{10}^-$ , the intensity slowly increases from 3.0 to 3.9 eV and reaches a distinct peak at 3.9 eV. The PES of  $V_3Si_{11}^-$  yields four peaks with increasing height. For the spectrum of  $V_3Si_{12}^-$ , a small broadened feature is seen from 2.5 to 3.0 eV and a peak appears over 4.0 eV. The first peak on the PES of  $V_3Si_{13}^-$  emerges very late (at 3.39 eV), followed by a broadened area and a distinct peak at over 4.0 eV. For  $V_3Si_{14}^-$ , a small broadened feature around 3.00 eV (VDE) appears and several more peaks come out after 3.3 eV.



All the VDEs and ADEs determined from photoelectron spectra in Figure 1 are summarized in Table 1. Overall speaking, VDE or ADE for a  $V_3Si_n^-$  cluster increases with the number ( $n$ ) of silicon atoms, whereas  $V_3Si_6^-$  and  $V_3Si_{12}^-$  show local minima. The detailed electronic properties will be discussed along with the theoretical calculations in section 3.3.

**3.2. Low-Energy Structures of  $V_3Si_n^-$  ( $n = 3-14$ ) Clusters.** The lowest-energy structures of  $V_3Si_n^-$  ( $n = 3-14$ ) clusters determined from GA-DFT global search are displayed in Figure 2, along with some important structural isomers for discussion.  $V_3Si_3^-$ -a has a  $C_s$  symmetry with  $V_3$  triangle at the center and three Si atoms being separated on the two sides. The V–V bond lengths are 2.160, 2.160, and 2.656 Å, respectively. The BL of Si–Si is 2.657 Å and the average V–Si BL is 2.457 Å. The metastable one,  $V_3Si_3^-$ -b, which is 0.313 eV higher in energy, has an octahedral structure and there are only two V–V bonds (both are 2.087 Å). In the structure of  $V_3Si_3^-$ -c isomer, three Si atoms join together to form a line while three V atoms constitute a triangle.

In the ground state structure of  $V_3Si_4^-$ , four Si atoms constitute a polyline and three V atoms fill in the empty positions, forming a face-capped square bipyramid. The  $V_3Si_4^-$ -b isomer lies 0.115 eV higher in energy and has a bicapped triangle bipyramid configuration, in which three V atoms form a triangle at the center and four Si atoms are separated into two dimers.  $V_3Si_4^-$ -c is a pentagonal bipyramid with two V atoms on the vertex, while the rest one V and four Si atoms make up of a pentagon.

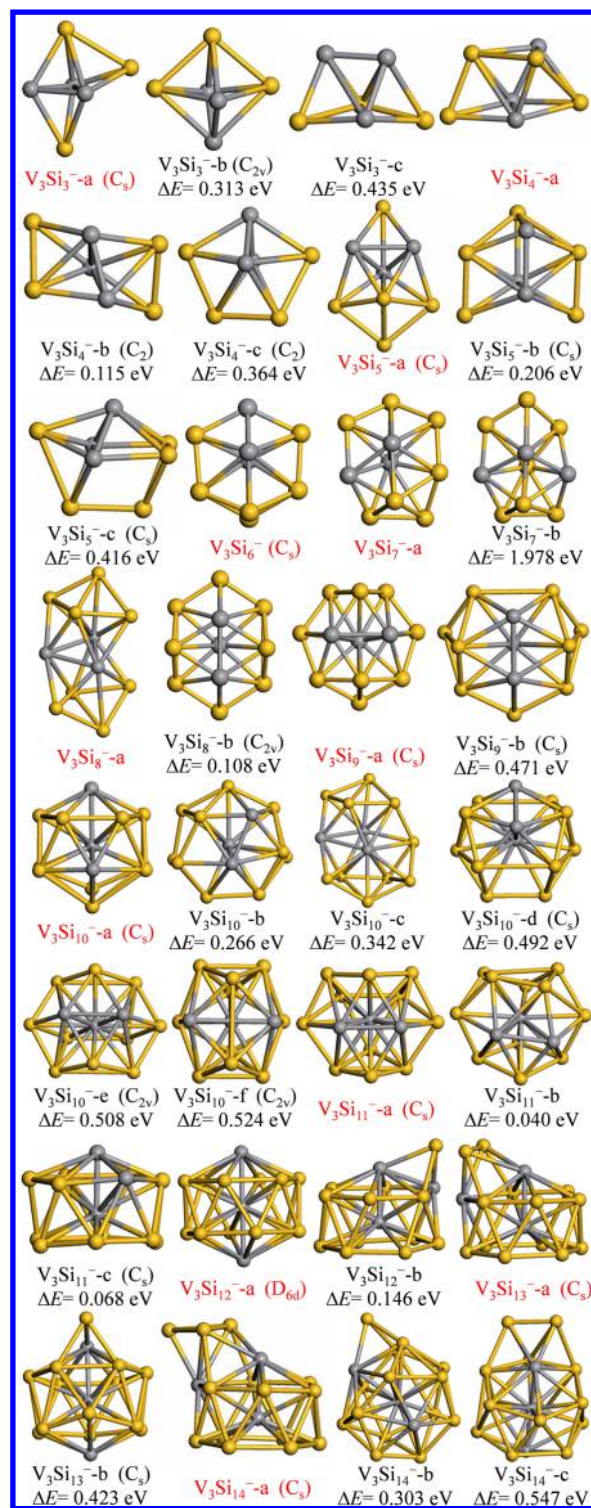
As the ground state, the geometry of  $V_3Si_5^-$ -a is a face-capped pentagonal bipyramid with slight distortion. The three V atoms form a triangle facet of the bipyramid, which is capped by a Si atom. In  $V_3Si_5^-$ -b isomer with  $\Delta E = 0.206$  eV, three V atoms and one Si atom constitute a quadrangle in the middle and the rest four Si atoms form two dimers and locate on the two sides.  $V_3Si_5^-$ -c structure consists of a square pyramid of  $Si_2V_3$  and a  $Si_3$  triangle and can be related to the most stable structure of  $V_3Si_6^-$ .

In  $V_3Si_6^-$ , three V atoms constitute a triangle with BL of 2.355 Å, 2.219 and 2.273 Å, respectively. This  $V_3$  triangle forms the basal plane for a trigonal bipyramid with two Si atoms on top and bottom. Another trigonal bipyramid ( $VSi_4$ ) is linked with this  $V_3Si_2$  one by sharing one V atom. The entire cluster exhibits oblate geometry with  $C_s$  symmetry. The average V–V BL is 2.282 Å, shorter than the average BLs of 2.617 Å for V–Si and 2.448 Å for Si–Si.

In the lowest-energy  $V_3Si_7^-$  anion cluster, three V atoms form an acute triangle, while an obtuse  $V_3$  triangle is found in isomer  $V_3Si_7^-$ -b, which is 1.978 eV higher in energy. These two structures indeed resemble each other; both having a trigonal bipyramid of  $V_3Si_2$  as a core surrounded by two and three Si atoms on the two sides.

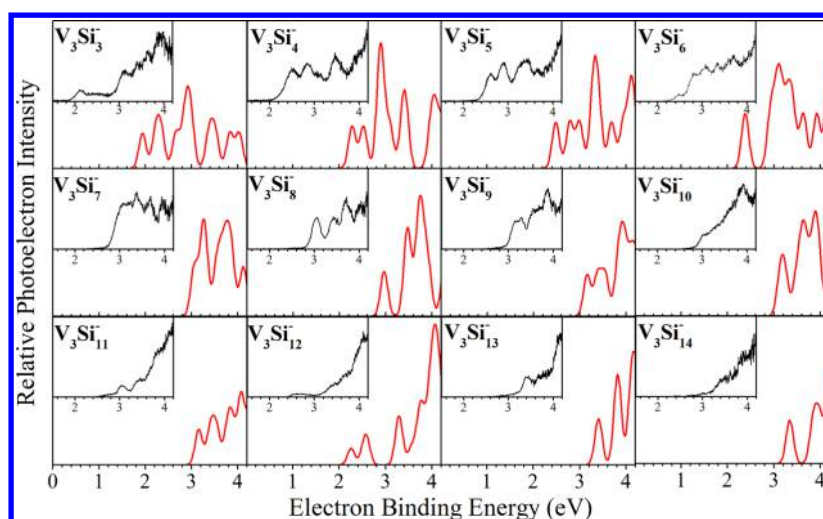
In the most stable structure of  $V_3Si_8^-$ -a, eight Si atoms are separated into two parts (each form a four-atom rhombus) by the middle  $V_3$  triangle. A more symmetric configuration ( $C_{2v}$ ) is obtained as the metastable isomer  $V_3Si_8^-$ -b with  $\Delta E = 0.108$  eV. It can be viewed as an open trigonal bipyramid of  $V_3Si_2$  in the middle capped with three Si atoms on each of the two sides. By capping one Si atom on the waist of  $V_3Si_8^-$ -b, the ground-state layered structure of  $V_3Si_9^-$  anion is obtained. Similarly,  $V_3Si_9^-$ -b can be seen as placing a Si atom on the  $V_3Si_8^-$ -a with some reconstruction.

For the  $V_3Si_{10}^-$  cluster, we found six low-lying isomers whose energy differences are in range of about 0.5 eV.  $V_3Si_{10}^-$ -a is a



**Figure 2.** Low-energy structures of  $V_3Si_n^-$  ( $n = 3-14$ ) clusters. For each cluster size, the energy difference of several isomers (marked as  $V_3Si_n^-$ -b,  $V_3Si_n^-$ -c, and so on) with regard to the lowest-energy one (marked as  $V_3Si_n^-$ -a) are given by  $\Delta E$ . The cluster symmetries are given in brackets (otherwise,  $C_1$ ). Gray and yellow balls represent V and Si atoms, respectively.

truncated V-centered icosahedron but with a hexagon instead of a pentagon on the bottom, whereas a distorted V-centered icosahedron ( $V_3Si_{10}^-$ -f) is 0.524 eV higher in energy.  $V_3Si_{10}^-$ -b,  $V_3Si_{10}^-$ -c, and  $V_3Si_{10}^-$ -d can all be constructed from  $V_3Si_8^-$ -a by adding two extra silicon atoms and fusing two parts. The 3–7–



**Figure 3.** Photoelectron spectra for  $V_3Si_n^-$  clusters ( $n = 3-14$ ) from ab initio calculations. The insets are experimental data from Figure 1 for comparison. A uniform Gaussian broadening of 0.08 eV is chosen for all the simulated spectra.

3 layered configuration of  $V_3Si_{10}^-$ -e comes from  $V_3Si_8^-$ -b by capping two Si atoms on the back side, preserving  $C_{2v}$  symmetry.

The lowest-energy structure of  $V_3Si_{11}^-$  is obtained by adding one Si atom to  $V_3Si_{10}^-$ -e, forming a 3-7-4 layered structure. With different arrangement of top five Si atoms, one can obtain a metastable structure of  $V_3Si_{11}^-$ -b with  $\Delta E = 0.04$  eV. Interestingly,  $V_3Si_{11}^-$ -c forms an incomplete V-center cage consisting of two hexagons (one with six Si atoms and the other with five Si atoms and one V atom) and one vertex V atom. This isomer is only less stable than the ground state by 0.068 eV.

As a continuation of  $V_3Si_{11}^-$ -c, the ground state configuration ( $D_{6d}$  symmetry) of  $V_3Si_{12}^-$ -a is composed of a central axis of  $V_3$  surrounded by two staggered  $Si_6$  hexagonal rings. This unique wheel-like structure has been reported in our recent publication.<sup>48</sup> Replacing one Si atom on the hexagonal ring by one V atom and capping this Si atom on the triangular face leads to the  $V_3Si_{12}^-$ -b isomer, whose energy is higher than the ground-state structure by 0.146 eV.

Starting from  $V_3Si_{12}^-$ -b,  $V_3Si_{13}^-$ -a can be constructed by further capping of an additional Si atom on the triangular face nearby the first capped Si atom. Capping one Si atom on the symmetric  $D_{6d}$  cage of  $V_3Si_{12}^-$ -a leads to  $V_3Si_{13}^-$ -b configuration; however, it is less stable by 0.423 eV probably due to distortion of the original 14-vertex cage.

$V_3Si_{14}^-$ -a follows the structural motif of  $V_3Si_{12}^-$ -b and  $V_3Si_{13}^-$ -a, which can be obtained by capping one additional Si atom on the upper lateral  $Si_2V$  triangle of  $V_3Si_{13}^-$ -a.  $V_3Si_{14}^-$ -b is a severely distorted V-centered cage face capped with one Si atom. Isomer  $V_3Si_{14}^-$ -c can be viewed as adding two Si atoms on  $V_3Si_{12}^-$ -a; however, the two additional Si atoms leads to significant deviation from the original  $D_{6d}$  symmetry of  $V_3Si_{12}^-$ -a cage.

Overall speaking, in the low-lying structures of  $V_3Si_n^-$  ( $n = 3-14$ ) clusters, vanadium atoms tend to bond with each other and form  $V_3$  triangle since V-V bond is stronger than V-Si bond, with the only exception at  $V_3Si_{12}^-$ -a. For all  $V_3Si_n^-$  clusters considered, the lengths of V-V bonds are in the range of 2.160–2.656 Å, moderately shorter than BLs of V-Si (2.360–2.695 Å) and Si-Si (2.414–2.657 Å). The smaller  $V_3Si_n^-$  clusters, with  $n = 3-9$  adopt flat-shape, while incomplete

cages with one V atom at the center form at  $V_3Si_{10}^-$  and  $V_3Si_{11}^-$ . A highly symmetric V-centered  $D_{6d}$  cage emerges at  $V_3Si_{12}^-$ , which also exhibits interesting ferrimagnetic behavior (magnetic moments on V atoms:  $2.4 \mu_B$ ,  $-0.6 \mu_B$ , and  $2.4 \mu_B$ , respectively).<sup>48</sup> The ground state structures of  $V_3Si_{13}^-$  and  $V_3Si_{14}^-$  can be obtained by capping Si atoms on the  $D_{6d}$  cage of  $V_3Si_{12}^-$  with the bottom atom truncated.

The present structural motifs of  $V_3Si_n^-$  clusters can be compared to the silicon clusters doped with one or two vanadium atoms. In the case of  $VSi_n$  clusters, 12 Si atoms are needed to completely surround the central vanadium atom, while open basket structures are preferred for  $n < 12$ . So far, little is known for the growth pattern of  $V_2Si_n$  clusters. For  $V_2Si_{12}^-$  cluster,<sup>48</sup> our recent PES combined DFT study revealed a structure with 12 Si atoms forming a hexagonal antiprism cage, one V atom in the cage center, and another V on the top. It was theoretically predicted that tube-like double hexagonal prism structure with some distortion is most stable for  $V_2Si_{18}$  cluster.<sup>44</sup> At last,  $V_2Si_{20}$  cluster has an elongated dodecahedron configuration with a  $V_2$  unit encapsulated inside  $Si_{20}$  cage, which is the smallest fullerene-like silicon cage.<sup>47</sup> Even with limited knowledge on the  $V_2Si_n$  clusters, it seems that coexistence of three vanadium atoms in the silicon framework results in different structural pattern with regard to those with only one or two vanadium dopants. Therefore, doping three or more transition metal atoms into silicon clusters would lead to new opportunities in tailoring the structural and electronic properties of the doped silicon clusters.

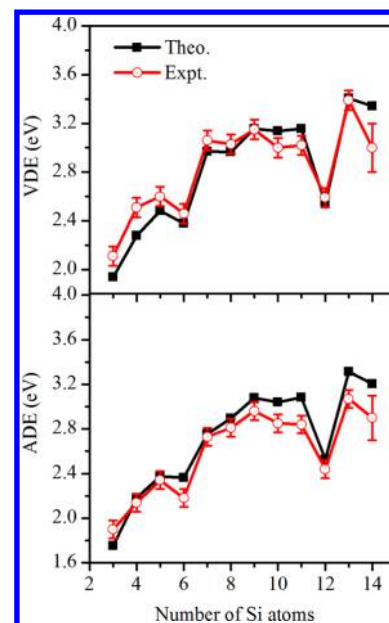
**3.3. Electronic Properties of  $V_3Si_n^-$  ( $n = 3-14$ ) Clusters with Ground-State Structures.** Based on the energy levels of anionic clusters, photoelectron spectra were simulated using the “generalized Koopman’s theorem”.<sup>64</sup> A nonvanishing energy shift of the energy levels is required for describing the asymptotic Kohn–Sham equations. With broadening the shifted energy levels, it provides a simple and efficient way to obtain the photoelectron spectra from the density of states. Generally, this viable method yields a faithful description of the experimental data, although it has ignored the true excited states of a cluster. Figure 3 displays the simulated photoelectron spectra for the lowest structures of  $V_3Si_n^-$  clusters ( $n = 3-14$ ) in Figure 2, along with the experimental spectra in Figure 1 for comparison. One can see satisfactory overall agreement



between simulated and measured spectra, demonstrating the validity of the present theoretical approaches.

For  $V_3Si_3^-$ , the simulated spectrum shows four discrete peaks and a broad one. Except for the first one that is different from the experimental results, the others agree well. In the simulated spectrum of  $V_3Si_4^-$ , it also has four main peaks as observed in the experimental PES, while the fifth peak comes out at 4.05 eV. Compared to experiment, the overall spectrum is slightly narrower and moved forward in energy. For  $V_3Si_5^-$ , the first peak locates at 2.48 eV and the following peak is broadened into two peaks. The essential characteristics of experimental PES are excellently reproduced by DFT calculation. In the simulated spectrum of  $V_3Si_6^-$ , the first two peaks are separated by a big valley while these peaks merge together in experimental spectrum. For  $V_3Si_7^-$ , a relatively narrower feature and two major peaks at 3.25 and 3.79 eV are obtained in the simulated spectrum. Such three-peak behavior is also seen in experiment. Similarly, three major peaks can be clearly found in the theoretical spectrum of  $V_3Si_8^-$  except for a small shift of  $\sim 0.1$  eV compared to the experimental data. The simulated spectrum of  $V_3Si_9^-$  presents the same tendency as the experimental one. The DFT simulation successfully reproduces the experimental trend and yields three obvious peaks at 3.19, 3.55, and 3.89 eV, except for a dip at 3.36 eV. For the PES of  $V_3Si_{11}^-$ , both DFT calculation and experiment yield four peaks with increasing height. The existing difference between theory and experiment might be attributed to the limited distinguish ability in experiment. Similar three-peak and two-peak behaviors occur in the  $V_3Si_{13}^-$  and  $V_3Si_{14}^-$  clusters, respectively. For the simulated PES of  $V_3Si_{12}^-$ , five peaks are centered at 2.24, 2.58, 3.30, 3.79, and 4.06 eV, respectively. The former two overlap with each other and the fourth one shows as a shoulder of the fifth peak. In short, we suspect that the discrepancy between theory and experiment is due to the limited experimental resolution, which leads to overlap of several peaks into a broad feature.

To further explore the electronic properties of  $V_3Si_n^-$  clusters, the measured and computed vertical detachment energies (VDEs) and adiabatic detachment energies (ADEs) of the cluster anions are plotted in Figure 4. In the experimental curve of VDEs, one can find an increasing trend from 2.0–3.4 eV, except for the local minima at  $V_3Si_6^-$ ,  $V_3Si_{12}^-$ , and  $V_3Si_{14}^-$ . The theoretical VDEs reproduce this trend generally well, whereas there is a noticeable overestimation (0.34 eV) at  $V_3Si_{14}^-$ . In general, the ADE of a cluster anion is equal to the adiabatic electron affinity (EA) of the corresponding neutral species when their geometries are close to each other. From experiment, one can find that ADE keep rising from 1.9–2.2 eV for  $V_3Si_n^-$  ( $n = 3-6$ ) and this trend becomes slowly in the range of 2.7–3.0 eV as the number of silicon atoms increases from 7 to 11. Afterward, the ADE shows an odd–even oscillation from  $n = 11$  to 14, with a local minimum at  $V_3Si_{12}^-$  ( $2.44 \pm 0.08$  eV). Again, the experimental tendency is well reproduced by ab initio simulation, with an overestimation of about 0.27 eV at  $V_3Si_{13}^-$  and  $V_3Si_{14}^-$ . In both ADE and VDE,  $V_3Si_{12}^-$  shows a distinct minimum with regard to its neighboring sizes. From both geometric and electronic points of view,  $V_3Si_{12}^-$  stands out as a unique species with high symmetry and appreciable stability. For a given neutral cluster, the lower EA corresponds to higher stability. In other words,  $V_3Si_{12}$  neutral cluster is stable. The details of this fascinating cluster have already been discussed in our recent publication.<sup>48</sup>



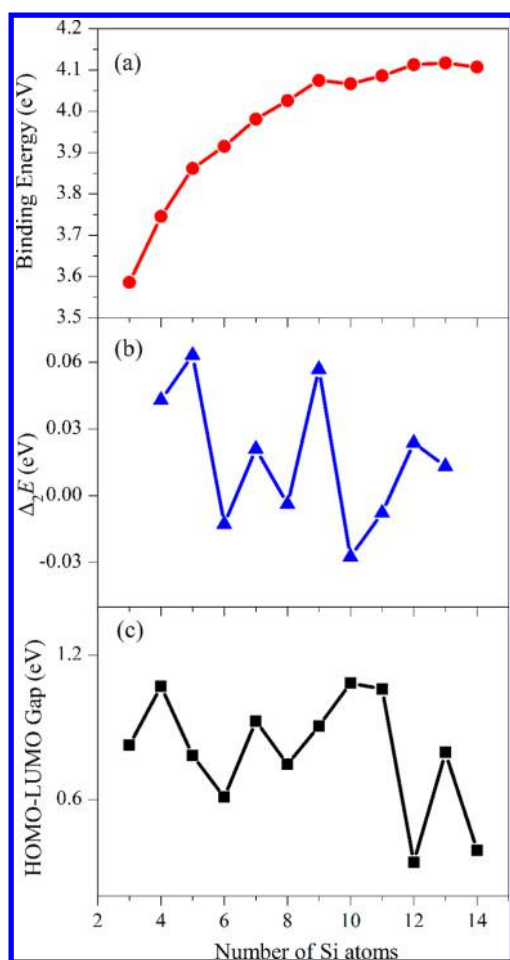
**Figure 4.** Vertical detachment energies (VDEs) and adiabatic detachment energies (ADEs) of  $V_3Si_n^-$  clusters: black squares, theory; red circles, experiment.

**3.4. Stabilities and HOMO–LUMO Gaps of  $V_3Si_n^-$  ( $n = 3-14$ ) Clusters.** In Figure 5a, we plot the binding energies of  $V_3Si_n^-$  clusters as a function of size  $n$ . For a  $A_xB_y$  cluster, its binding energy is defined by  $E_b(A_xB_y) = (E(A_xB_y) - xE(A) - yE(B))/(x + y)$ , where  $E(A_xB_y)$  is the energy of  $A_xB_y$  cluster,  $E(A)$  or  $E(B)$  is the energy per single atom of element A or B in the vacuum,  $x$  or  $y$  is the number of A or B atoms in the cluster. The binding energy gradually increases with growing number of Si atoms, suggesting the formation of a cluster is more and more easy as it becomes bigger. To examine the relative stability, the second order energy differences ( $\Delta_2E$ ) of the clusters in their ground-state geometries are calculated and plotted in Figure 5b. One can see three peaks at  $V_3Si_5^-$ ,  $V_3Si_9^-$ , and  $V_3Si_{12}^-$ , indicating that they are more stable than their neighboring sized clusters. The high stability of  $V_3Si_{12}^-$  can be related to its high symmetry, closed cage configuration, and lower VDE or ADE.

As shown in Figure 5c, the HOMO–LUMO gaps of  $V_3Si_n^-$  clusters range between 0.4 and 1.2 eV.  $V_3Si_4^-$ ,  $V_3Si_{10}^-$ , and  $V_3Si_{11}^-$  possess relatively higher gaps while the gaps of  $V_3Si_6^-$ ,  $V_3Si_{12}^-$ , and  $V_3Si_{14}^-$  are lower. We also compare these gap values to the pure neutral silicon clusters with same total number of atoms from DFT calculations, whose amplitudes are between 0.86 and 2.21 eV.<sup>65</sup> On average, replacing three Si atoms by V atoms reduces the gap by  $\sim 1.1$  eV.

## 4. CONCLUSIONS

Using a linear time-of-flight mass spectrometer and a magnetic-bottle photoelectron spectrometer, we generated  $V_3Si_n^-$  ( $n = 3-14$ ) clusters in a laser vaporization source and recorded their photoelectron spectra. Meanwhile, using an unbiased genetic algorithm, we globally searched the low-energy structures of these  $V_3Si_n^-$  clusters. For each cluster, the three V atoms tend to form triangle surrounded by Si atoms. Accordingly, the average length of V–V bonds of about 2.3 Å is 0.3 Å shorter than that of V–Si. An exception case was found at  $V_3Si_{12}^-$ , which has a wheel-like  $D_{6d}$  structure with a central  $V_3$  axis and



**Figure 5.** Binding energies (a), second-order of energy differences ( $\Delta_2 E$ ) (b), and HOMO–LUMO gaps (c) of  $V_3Si_n^-$  ( $n = 3–14$ ) clusters.

exhibits ferrimagnetism. The agreement of PES, ADE, and VDE between experiments and theoretical calculations are satisfactory. In particular, the size-dependent trends of ADE and VDE are well reproduced by ab initio calculations, confirming that we have located the correct ground state configurations of these  $V_3Si_n^-$  clusters.

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### Notes

The authors declare no competing financial interest.

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