# Electronic and geometrical structure of Mn<sub>13</sub> anions, cations, and neutrals

G. L. Gutsev,  $^{1,a)}$  M. D. Mochena,  $^1$  Charles W. Bauschlicher, Jr.,  $^2$  W.-J. Zheng,  $^3$  O. C. Thomas,  $^3$  and Kit H. Bowen  $^{3,a)}$ <sup>1</sup>Department of Physics, Florida A&M University, Tallahassee, Florida 32307, USA

<sup>2</sup>Mail Stop 230-3, NASA Ames Research Center, Moffett Field, California 94035, USA

<sup>3</sup>Department of Chemistry and Department of Materials Science, Johns Hopkins University, Baltimore, Maryland 21218, USA

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We have computed the electronic and geometrical structures of thirteen atom manganese clusters in all three charge states,  $Mn_{13}^-$ ,  $Mn_{13}^+$ , and  $Mn_{13}$  by using density functional theory with the generalized gradient approximation. Our results for  $Mn_{13}^-$  are compared with our anion photoelectron spectrum of  $Mn_{13}^-$ , published in this paper. Our results for  $Mn_{13}^+$  are compared with the previously published photoionization results of Knickelbein [J. Chem. Phys. 106, 9810 (1997)]. There is a good agreement between theoretical and experimental values of ionization and electron attachment energies. © 2008 American Institute of Physics. [DOI: 10.1063/1.2956494]

## **I. INTRODUCTION**

Manganese clusters,  $Mn_n$ , are intriguing species<sup>1,2</sup> whose ground states undergo a ferro- to ferrimagnetic transition<sup>3,4</sup> as the number of atoms, n, increases. The size of the cluster for which the transition occurs depends on the charge and equals 5, 6, and 3 in the neutral,<sup>3,4</sup> anionic,<sup>5</sup> and cationic<sup>5</sup> series, respectively. In addition, Mn<sub>5</sub> and Mn<sub>6</sub> were found to possess noncollinear local magnetic moments on the atoms.<sup>6–9</sup> Noncollinear magnetic structure studies have been extended to larger clusters (up to Mn<sub>8</sub> in Ref. 10, up to Mn<sub>19</sub> in Ref. 11, and up to  $Mn_{55}$  at the bulk-type geometries in Ref. 12).

On the experimental side, anion photoelectron spectra<sup>13</sup> were obtained for  $Mn_n^-$ , n=3-8. They showed an increase in electron detachment energies with increasing n. Also, ionization energies were previously measured<sup>14</sup> for  $Mn_n$  clusters in the range of  $7 \le n \le 64$ . While a generally monotonic decrease in ionization energies (from 5.44 to 4.37 eV) was observed, deviations from this trend were seen at the smallest sizes, as well as at n=13 and 19. Stern–Gerlach experiments were performed for  $Mn_n$  clusters in the ranges of  $11 \le n$  $\leq 99$  (Ref. 15) and  $5 \leq n \leq 22$ .<sup>16</sup> The largest differences in the magnetic moment per atom of  $Mn_n$ , with respect to  $Mn_{n-1}$  and  $Mn_{n+1}$ , were observed at n=13 and 19. Furthermore, optical spectra were obtained<sup>17</sup> for the  $Mn_3^+$  trimer, and dissociation energies were measured  $^{18,19}$  for  $Mn_2^+$  to  $Mn_7^+$ .

The ground state of neutral  $Mn_{13}$  was found<sup>20</sup> to possess an icosahedral geometrical structure, which is typical for several other 3*d*-metal clusters  $M_{13}$  such as  $Sc_{13}^{21}$  Ti<sub>13</sub><sup>22</sup> and  $Fe_{13}$ .<sup>23</sup> Mn<sub>13</sub> icosahedrons are also found to be the building units in the bulk GaMn compounds.<sup>24</sup> The magnetic moment per atom obtained by Nayak et al.<sup>20</sup> is  $2.54 \mu_B$ , while the experimental value, which was measured later, is  $0.54 \pm 0.06 \mu_B$ .<sup>16</sup> Kawazoe *et al.*<sup>25</sup> confirmed that the ground state structure is icosahedral and obtained the magnetic moment of  $0.23\mu_B$  per atom. Subsequent studies<sup>26,27</sup> arrived at the same structure, magnetic moment, and distributions of spin-up and spin-down excess electron density as those found by Kawazoe et al.<sup>25</sup>

Our present work combines an experimental anion photoelectron spectroscopy study of the Mn<sub>13</sub> anion and a theoretical search for the lowest total energy isomers of Mn<sub>13</sub> and  $Mn_{13}^+$ . Geometrical optimizations were performed over a wide range of the spin multiplicities using all-electron density functional theory with generalized gradient approximation and flexible basis sets. After discussing both the experimental and theoretical methods and procedures used in this work, we present our experimental data on  $Mn_{13}^-$  and then compare it, along with the previous data<sup>12</sup> on  $Mn_{13}^+$ , to our theoretical results, including geometrical structures and excess electron densities as well as the electron affinity (EA<sub>ad</sub>) and the ionization potential (IP) of  $Mn_{13}$ .

### **II. EXPERIMENTAL METHODS**

Anion photoelectron spectroscopy is conducted by crossing a beam of mass-selected negative ions with a fixedfrequency photon beam and energy analyzing the resultant photodetached electrons. The photodetachment process is governed by the energy-conserving relationship,  $h\nu$ =EBE +EKE, where  $h\nu$  is the photon energy, EBE is the electron binding energy, and EKE is the electron kinetic energy. Briefly, our apparatus consists of an ion source, a linear timeof-flight mass analyzer (TOF-MS), a Nd:YAG photodetachment laser, and a magnetic bottle photoelectron spectrometer (MB-PES). The instrumental resolution of the MB-PES is  $\sim$ 35 meV at 1 eV EKE. The third (355 nm, 3.49 eV) harmonic of a Nd:YAG was used to photodetach electrons from the cluster anions of interest. Photoelectron spectra were calibrated against the well-known transitions of the Cu<sup>-</sup> anion. Manganese cluster anions were generated in a laser vaporization source in which a rotating, translating manganese rod was irradiated with 532 nm (2.33 eV) pulses from a second Nd:YAG laser, while nearly simultaneously bursts of

<sup>&</sup>lt;sup>a)</sup>Authors to whom correspondence should be addressed. Electronic mail: gennady.gutsev@famu.edu; kbowen@jbu.edu.

helium gas ( $\sim$ 3 atm) from the rear of the source were passing over the manganese rod. The rapidly expanding gas cooled the resulting plasma and generated the manganese cluster anions.

#### **III. COMPUTATIONAL METHODS AND PROCEDURES**

Computations were performed using the GAUSSIAN 03 (Ref. 28) programs system. The primary basis set used is  $6-311+G^{*}$ ,<sup>29</sup> (15s11p6d1f)/[10s7p4d1f], while the 6-311 +G(2d) basis set, (15s11p6d2f)/[10s7p4d2f], was used for estimating the dependence of the results obtained on f-function extensions. As in our previous work on Mn and iron clusters<sup>5,30</sup> we choose the BPW91 method, where the exchange-correlation functional is comprised of the Becke's exchange<sup>31</sup> and Perdew–Wang's correlation.<sup>32</sup> This preference is based on the results of our calibration calculations<sup>33</sup> on the  $Fe_4$  cluster performed by six different DFT methods. While providing similar spectroscopic constants as the other methods, the BPW91 method was found to be less sensitive to a numerical integration grid used in computations of the exchange and correlation contributions. This allows us to use less computationally demanding integration grids. A comprehensive comparison of semilocal and hybrid density functionals is beyond the scope of this work, but may be found elsewhere.34

We assume a collinear treatment of the magnetic structure. According to the most recent study,<sup>11</sup> the lowest energy collinear structure of  $Mn_{13}$  with the spin multiplicity of 4 is degenerate in total energy with the lowest non-collinear structure, which justifies our collinear computations.

We performed searches of the lowest energy states whose geometrical configurations possessed icosahedron and nonicosahedron topologies. The  $Mn_{13}$  nonicosahedron geometries depend strongly on the spin multiplicity of the electronic state and generally are very similar to the geometries of the lowest excited states found<sup>23</sup> for Fe<sub>13</sub>. Some other  $Mn_{13}$  states were considered previously,<sup>26</sup> but no state was closer than 0.89 eV to the icosahedral ground state.

A search for the lowest energy ferrimagnetic state is rather complicated,<sup>35</sup> because there are a larger number of possible orientations of the excess spin-up and spin-down densities. For ferrimagnetic trial guesses, we used spin-up and spin-down combinations produced in computations on singly and doubly charged ferrimagnetic  $Mn_{13}$  and  $Fe_{13}$  ions. We also created Mn<sub>13</sub> guess vectors by superimposing Mn atom vectors, where the spin-up and spin-down occupation for each atom in the cluster was set by hand. Each geometry optimization was followed by an analytical second derivatives calculation of the harmonic vibrational frequencies in order to confirm that the optimized geometry corresponds to a minimum. The total energies obtained were used to evaluate the adiabatic electron attachment (electron affinity) and detachment (ionization potential) energies of Mn<sub>13</sub>. The zeropoint vibrational energies are similar for ground-state Mn<sub>13</sub> (0.324 eV),  $Mn_{13}^{-}$  (0.319 eV), and  $Mn_{13}^{+}$  (0.322 eV) and were neglected in these calculations. Excess electron spin densities on atoms were obtained using natural atomic orbital populations (NAO) as implemented in the NBO suite.<sup>36</sup>

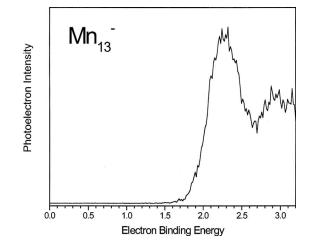


FIG. 1. Photoelectron spectrum of  $Mn_{13}^-$  measured with 3.49 eV photons.

#### **VI. RESULTS AND DISCUSSION**

#### A. Photoelectron spectrum of Mn<sub>13</sub>

Our anion photoelectron spectrum of Mn<sub>13</sub> measured with 3.49 eV photons is shown in Fig. 1. Its average vertical detachment energy, VDE, is  $2.2 \pm 0.1$  eV. The VDE is the EBE of the maximum in the lowest EBE spectral band. It is the EBE of the maximal Franck-Condon overlap in the photodetachment transition between the ground state of the Mn<sub>13</sub> anion and the ground state of its corresponding Mn<sub>13</sub> neutral. The adiabatic electron affinity, EA<sub>ad</sub>, is estimated to be  $1.9 \pm 0.1$  eV. The EA<sub>ad</sub> value is taken from the fast rising portion of the low EBE side of the lowest EBE band just above threshold. The EA<sub>ad</sub> is defined as the energy difference between the lowest vibrational level of the anion's ground electronic state and the lowest vibrational level of the ground electronic state of its neutral counterpart. The second band centered around  $\sim 2.9$  eV is the result of a photodetachment transition from the ground state of the  $Mn_{13}^-$  anion to an excited state of the Mn<sub>13</sub> neutral.

# B. Geometrical configurations and excess spin densities

The lowest total energy configurations of neutral  $Mn_{13}$  with different excess spin density patterns are presented in Fig. 2. As is seen, there are a large number of states within 0.3 eV of the ground state. To aid in an understanding of the origin of the states, the atoms with an excess spin up density are shaded dark, while those with an excess spin down density are shaded light. It is interesting to note that the lowest energy states may arise from different distributions of the spin density patterns. For example, while the lowest states with 2S+1=4 and 2S+1=6 have the same spin patterns, the lowest 2S+1=2 state has a different spin pattern as the lowest states with 2S+1=4 and 2S+1=6.

The spin multiplicity and excess spin density pattern obtained for the ground state of  $Mn_{13}$  is similar to that found by Kawazoe *et al.*<sup>25</sup> and in subsequent work.<sup>26,27</sup> The magnetic moment per atom is computed as twice the total spin divided by the number of atoms and is  $0.23\mu_B$  in the  $Mn_{13}$  ground

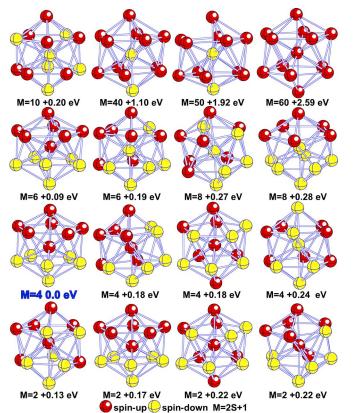


FIG. 2. (Color online) Excess spin density patterns in the lowest energy states of different spin multiplicities of neutral  $Mn_{13}$ . Energy separations are given with respect to the ground state total energy. The atoms with excess spin up density are shaded dark, while those with excess spin down density are shaded light.

state, which is substantially smaller than the experimental value of  $0.54 \pm 0.06 \mu_B$ .<sup>16</sup> This discrepancy may be related to omitting the orbital moment contribution since the total magnetic moment M=2S+L. According to the results of computations performed<sup>37</sup> for Ni<sub>n</sub> clusters using a model Hamiltonian, the orbital moment contribution may represent 20%–40% of the total magnetization and is therefore important for comparing theory and experiment. On the other hand, the neutral state with 2S+1=6 is higher than the ground state by 0.087 eV only. If this state was involved in Knickelbein's experiment<sup>16</sup> then the discrepancy is significantly reduced.

The search for the lowest energy states of  $Mn_{13}^-$  and  $Mn_{13}^+$  was performed using the neutral electronic densities of states presented in Fig. 2 as initial guesses, as well as using the converged electronic densities of the anion in optimizations of the cation and vice versa. The relative energies obtained in all three series are presented in Fig. 3. As is seen, there are a number of states that are close in total energy with the same or different spin multiplicities. The lowest energy states found for the anion and cation have the spin multiplicity of 3 and 5, respectively, and these states possess the same excess spin density pattern as the neutral ground state. The same spin multiplicity of  $Mn_{13}^{-1}$  was obtained in the recent pseudopotential calculations.<sup>38</sup>

The detailed structures of the  $Mn_{13}$ ,  $Mn_{13}^-$ , and  $Mn_{13}^+$  ground states are presented in Fig. 4. The ground states of

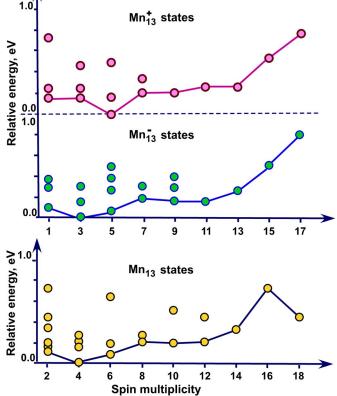


FIG. 3. (Color online) Total energy shifts of the  $Mn_{13}^-$  and  $Mn_{13}^+$  isomers with different spin multiplicity given with respect to the corresponding ground states.

both neutral and anion have  $C_{5v}$  symmetry while the cation ground state has  $C_1$  symmetry. In order to gain insight into asymmetry of spin-up ( $\alpha$ ) and spin-down ( $\beta$ ) excess spin density distributions in the neutral ground state, consider the results of the NAO population analysis presented in Table I. As is seen, the total effective atomic electron configurations are close to  $(3d^{6}4s^{1})$ , except for the central atom with  $(3d^{7.5}4s^{1})$ . The central atom population probably suffers from some population artifacts due to the large overlap population; therefore, we believe all atoms have a  $(3d^{6}4s^{1})$ occupation. In the atomic case, the promotion Mn  ${}^{6}S(3d^{5}({}^{6}S)4s^{2}) \rightarrow Mn {}^{6}D(3d^{6}({}^{5}D)4s^{1})$  requires<sup>39</sup> 2.15 eV and is the largest among the 3*d* atoms.

An inspection of Fig. 4 shows that the excess spin on the central atom is significantly smaller then those on the surface, suggesting that the spin coupling of the *d* shell has changed from  ${}^{5}D$  to allow additional bonding with the surface atoms. An inspection of Morse<sup>39</sup> shows that such a spin recoupling of the 3*d* shell requires significant energy, but since only one atom is involved, it appears to be favorable.

Attachment of an extra electron influences mostly the apex atoms whose distances from the central atom are affected more than those of the ring atoms. The excess spin density of the top apex atom decreases by 0.5e<sup>-</sup>, while the excess spin-down densities of the bottom ring atoms uniformly decreases by 0.1e<sup>-</sup> (see Fig. 4). This results in the decrease of the total spin by one. The hole formed due to the electron detachment is delocalized over the cluster, mostly affecting the atoms with the spin-up excess spin density.

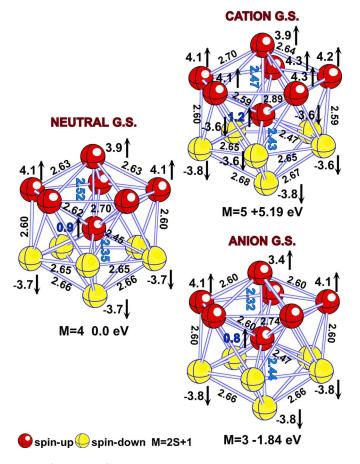


FIG. 4. (Color online) Geometrical configurations and excess spin densities of the ground-state  $Mn_{13}$ ,  $Mn_{13}^-$ , and  $Mn_{13}^+$  clusters. Bond lengths are in Å; excess spin densities are in electrons.

# C. Electron detachment from $Mn_{13}^-$ and ionization of $Mn_{13}$

Experimentally, ionization processes, whether from anions or neutrals, correspond to vertical processes. If one assumes that electron detachment and ionization are oneelectron processes, then the final spin multiplicities will differ by  $\pm 1$  from the spin multiplicity of the initial states involved in the process. Using the 6-311+G(2d) basis set, we calculated the EA<sub>ad</sub>, VDE, and IP values of Mn<sub>13</sub> and Mn<sub>13</sub><sup>-</sup>. (EA<sub>ad</sub> and IP values are properties of neutrals, while VDE is a property of anions.)

To calculate the adiabatic electron affinity of  $Mn_{13}$ , we computed the energy difference between the optimized anion geometry and the optimized neutral geometry. (This quantity could also be referred to as the adiabatic detachment energy of  $Mn_{13}^-$ .) The value of  $EA_{ad}$  that we computed was 1.84 eV, in close agreement with our experimentally determined value

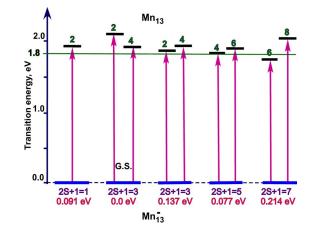


FIG. 5. (Color online) Energies of the vertical electron transition energies from the ground and four lowest energy excited states of the  $Mn_{13}^-$  anion. The energy shifts with respect to the ground state total energy are given below the spin multiplicities of the states involved.

of 1.9 eV. To calculate the VDE and other higher energy vertical transition energies of  $Mn_{13}^-$ , we computed the energy difference between the anion and neutral at the geometry of the  $Mn_{13}^-$  anion. Vertical transition energies from several lowest energy states of  $Mn_{13}^-$  are shown in Fig. 5. The  $Mn_{13}^-$  anion's ground state (labeled G.S.) has the spin multiplicity 2S+1=3. The two lowest vertical electron transition energies are 1.92 and 2.12 eV (from 2S+1=3 to 2S+1=4 and from 2S+1=3 to 2S+1=2, respectively). These energies are rather close to each other and, along with Franck–Condon broadening, the width of the main band in the spectrum due to some degree of structural difference between the anion and its neutral, probably contribute to the width of the main band in the spectrum. Given this, agreement with the experimental VDE value of 2.2 eV is quite satisfactory.

Experimental ionization spectra obtained<sup>14</sup> for  $Mn_{13}$ shows two ionization energies, one at  $4.82 \pm 0.05$  eV and the other one at  $5.30 \pm 0.05$  eV. The experiment was interpreted in terms of the presence of two  $Mn_{13}$  isomers. Vertical transition energies from several of the lower energy states of neutral  $Mn_{13}$  are shown in Fig. 6. We found vertical electron transitions from the neutral  $Mn_{13}$  ground state, 2S+1=4 to 2S+1=5 of  $Mn_{13}^+$  and to 2S+1=3 of  $Mn_{13}^+$  to be 5.26 and 5.39 eV, respectively. These are in good agreement the experimental value of 5.30 eV. Our computed value for the adiabatic ionization potential of  $Mn_{13}$  is 5.19 eV. In order to find an isomer that can be responsible for the value of 4.82 eV, we computed the vertical ionization energies for several excited states of  $Mn_{13}$ , including icosahedral and nonicosahedral isomers. The results of our computations for

TABLE I. NAO effective electronic configurations obtained for five types of atoms in the ground state of Mn<sub>13</sub>.

Atoms	Total	Spin up	Spin down	Excess
Central	$3d^{7.53}4s^{0.97}4p^{0.15}$	$3d^{4.24}4s^{0.48}4p^{0.07}$	$3d^{3.29}4s^{0.49}4p^{0.08}$	0.9
Ring spin up	$3d^{5.86}4s^{0.93}4p^{0.07}$	$3d^{4.85}4s^{0.57}4p^{0.05}$	$3d^{1.01}4s^{0.35}4p^{0.02}$	4.1
Apex spin up	$3d^{6.05}4s^{0.80}4p^{0.08}$	$3d^{4.92}4s^{0.46}4p^{0.05}$	$3d^{1.13}4s^{0.33}4p^{0.03}$	3.9
Ring spin down	$3d^{5.94}4s^{0.86}4p^{0.05}$	$3d^{1.13}4s^{0.41}4p^{0.02}$	$3d^{4.80}4s^{0.44}4p^{0.04}$	-3.7
Apex spin down	$3d^{6.08}4s^{0.87}4p^{0.06}$	$3d^{1.24}4s^{0.39}4p^{0.03}$	$3d^{4.85}4s^{0.47}4p^{0.03}$	-3.7

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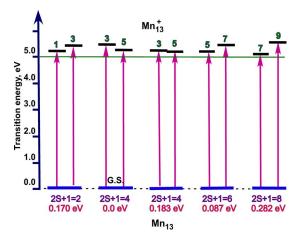


FIG. 6. (Color online) Energies of the vertical electron ionization energies from the ground and four lowest energy excited states of neutral  $\rm Mn_{13}.$ 

icosahedral isomers are presented in Fig. 6. The lowest ionization energy of 5.08 eV is found for the 2S+1=8 state, which is 0.28 eV above the ground state. The vertical IPs from nonicosahedral isomers are also found around 5.30 eV. Therefore, a further effort is required to find an isomer responsible for the lower energy transition in the experimental ionization spectra.

### V. CONCLUDING REMARKS

The results of the present  $Mn_{13}$  calculations are consistent with previous work for the spin multiplicity and overall distribution of spin up and spin down excess spin densities. As found in previous work, our magnetic moment per atom is  $0.23\mu_B$ , which is substantially smaller than the experimental value of  $0.54 \pm 0.06\mu_B$ .<sup>16</sup> Our measured vertical detachment energy, VDE, is  $2.2 \pm 0.1$  eV and the adiabatic electron affinity is estimated to be  $1.9 \pm 0.1$  eV. Our computed results are in good agreement with experiment giving support to the determination of both the ground state of the neutral and anion. Our computed IP is in good agreement with the larger experimental value of Knickelbein, but our results give no insight in the smaller experimental IP, which was interpreted as arising from an excited  $Mn_{13}$  isomer.

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